

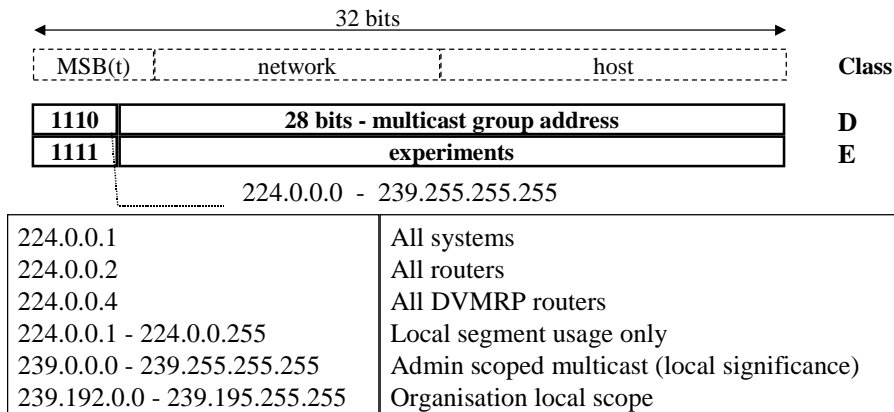
# Multicast routing principles in Internet

Motivation  
Recap on graphs  
Principles

## Multicast capability has been and is under intensive development in the 1990's

- MBONE used to multicast IETF meetings from 1992
- Extends LAN broadcast capability to WAN in an efficient manner
- Valuable applications
  - resource discovery
  - network load minimization by replacing many pt-to-pt transmissions
  - multimedia conferencing

## Multicast addresses

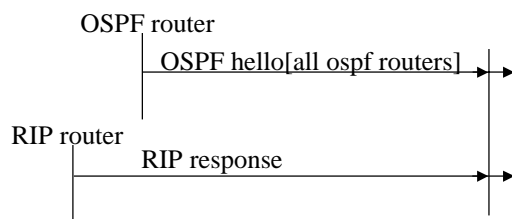


Ethernet MAC address: MACprefix+G --> no lookup, no ARP

Note: + Sender does not need to belong to G.

+ Address space is flat!

## Resource discovery by MC simplifies network management

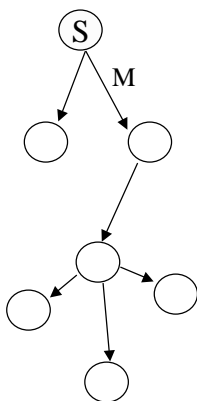


- No need for lists of neighbors, just use std MC address
- How to find corporate DNS -server --> MC to all nodes in corporate network.
- Network is easily flooded with messages.
- TTL can be used for Broadcast scope limitation
  - > find nearest DNS or whatever
  - when TTL=0, router does not return ICMP msg!

## Conferencing requirements include

- Multiple sources, multiple recipients, multiple media
- Variable membership
- Small conferences with intelligent media control (what is sent to where)
- Large conferences require media processing in special devices

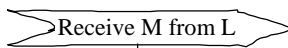
## Multipoint sessions differ from point-to-point communication



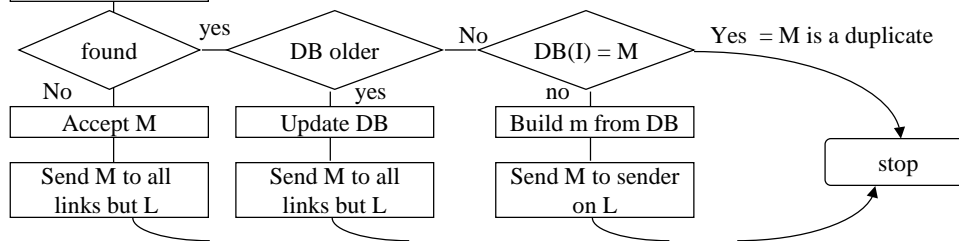
- Participants may join and leave the session.
- Receiver-makes good principle instead of session parameter negotiation.
- Window based flow control does not apply:  
-- use UDP / connectionless protocols

## Flooding is the simplest MC algorithm

Flooding algorithm is



- Need to keep state (DB) in nodes!
- No group membership: target is all nodes



- Examples: OSPF, usenet news...

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## Alternative to DB in flooding is trace info in the message

- Trace info in Message lists all passed nodes
- Avoids a costly DB reads but may accept same M several times.
- If neighbor is in trace, does not send

★ *Flooding guarantees that node will not forward the same packet twice. It does not guarantee that node will receive the same packet only once! --> Greedy algorithm.*  
 +++*Does not depend on routing tables --> robust*

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## Networks are modeled as Graphs.

$$G = (V, E),$$

$V$  - set of **vertices or nodes** (non-empty, finite set)

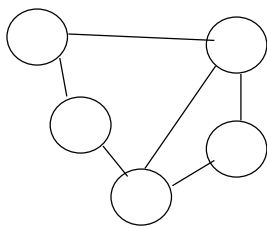
$E = \{e_j \mid j = 1, 2, \dots, M\}$  - set of **edges or links**.

$$e_j = (v_i, v_k) = (i, k)$$

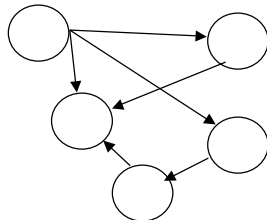
Nodes  $i$  and  $k$  are **adjacent** if link  $(i, k)$  exists.

Nodes  $i$  and  $k$  are also called **neighbors**.

## Links are bi-, arcs are unidirectional



Undirected graph

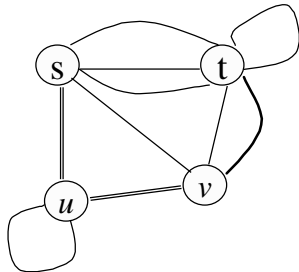


Directed graph

**Degree of a node** is the number of its neighbors or the number of links **incident on the node**.

Unidirectional links,  $a_j = (v_i, v_k) = [i, k]$  are called **arcs**. If links and nodes have properties, the graph is called a **network**.

## Graphs with parallel links are called multigraphs



Links between a node and itself are **self loops**.

Graph with no parallel links and no self loops is a **simple graph**.

A **path** in a network is a sequence of links beginning at some node  $s$  and ending at some node  $t$ . =  **$s,t$ -path**.  
If  $s = t$ , path is called a **cycle**. If an intermediate node appears no more than once, it is a **simple cycle**.

## Graph is **Connected** if there is at least one path between every pair of nodes.

- A subset of nodes with paths to one another is a connected component.

Reflective: By def.  $\exists i,i$ -path

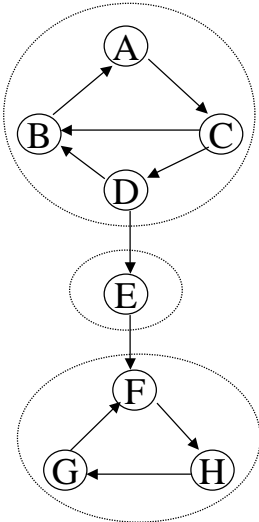
Symmetric:  $\exists i,j$ -path  $\Rightarrow \exists j,i$ -path

Transitive:  $\exists i,j$ -path and  $\exists j,k$ -path  $\Rightarrow \exists i,k$ -path

$\Rightarrow$  Components are equivalence classes and the component structure is a partition of the graph.

Partition applies to links and nodes alike.

A directed graph is **strongly connected** if there is a **directed path** from every node to every other node.



- Directed connectivity is not symmetric.
- A subset of nodes with directed paths from any one node to any other is a **strongly connected component**.
- A node belongs to exactly one strongly connected c. An arc is part of *at most one* strongly connected c.

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A **tree** is a graph without cycles

- Given a Graph  $G = (V, E)$ ,  $H$  is a subgraph of  $G$  if  $H = (V', E')$  where  $V' \subset V$  and  $E' \subset E$
- A **spanning tree** is a connected graph without cycles.
- If graph is not necessarily connected, we talk about a **forest**.

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## Spanning trees model minimally connected networks

- ST is a minimum cost network.
- Only a single path exists between any two nodes in a ST --> routing is trivial.
- If a graph has  $N$  nodes, any tree spanning the nodes has exactly  $N - 1$  edges.
- Any forest with  $k$  components has exactly  $N - k$  edges. (proof by induction starting from graph with no edges).

A set of edges whose removal disconnects a graph is called a **disconnecting set**.

- **XY-cutset** partitions a graph to subgraphs  $X$  and  $Y$ .
- In a tree any edge is a **minimal cutset**.
- A minimal set of nodes whose removal partitions the remaining nodes into two connected subgraphs is called a **cut**.



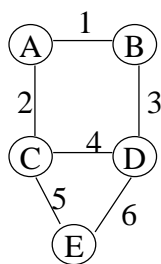
## Suomalaiset graafitermit

|                       |  |                      |                          |
|-----------------------|--|----------------------|--------------------------|
| Vertex, node          | - kärki, solmu                         | Subgraph             | - aligraafi              |
| Edge, link            | - syrjä, linkki, sivu,<br>kaari, haara | Tree                 | - puu                    |
| Adjacent              | - viereinen                            | Spanning tree        | - virittäjäpuu           |
| Neighbor              | - naapuri                              | Forest               | - metsä                  |
| Degree of<br>a node   | - solmun aste(?)                       | Disconnecting<br>set | - erotusjoukko           |
| Arc                   | - kaari                                | Cut                  | - leikkaus               |
| Cycle, Loop           | - silmukka                             | XY-cutset            | - XY-leikkaus-<br>joukko |
| Path                  | - polku                                |                      |                          |
| Directed path         | - suunnattu polku                      |                      |                          |
| Connected             | - yhteydellinen, yhdistetty            |                      |                          |
| Strongly<br>connected | - vahvasti yhteydellinen               |                      |                          |

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## Adjacency and Incidence Matrices are used to present Graphs



|      |   | Node |   |   |   |   |
|------|---|------|---|---|---|---|
|      |   | A    | B | C | D | E |
| Node | A | 0    | 1 | 1 | 0 | 0 |
|      | B | 1    | 0 | 0 | 1 | 0 |
|      | C | 1    | 0 | 0 | 1 | 1 |
|      | D | 0    | 1 | 1 | 0 | 1 |
|      | E | 0    | 0 | 1 | 1 | 0 |

Adjacency Matrix

For an undirected graph  
Adjacency matrix is symmetric.

|      |   | Link |   |   |   |   |   |
|------|---|------|---|---|---|---|---|
|      |   | 1    | 2 | 3 | 4 | 5 | 6 |
| Node | A | 1    | 1 | 0 | 0 | 0 | 0 |
|      | B | 1    | 0 | 1 | 0 | 0 | 0 |
|      | C | 0    | 1 | 0 | 1 | 1 | 0 |
|      | D | 0    | 0 | 1 | 1 | 0 | 1 |
|      | E | 0    | 0 | 0 | 0 | 1 | 1 |

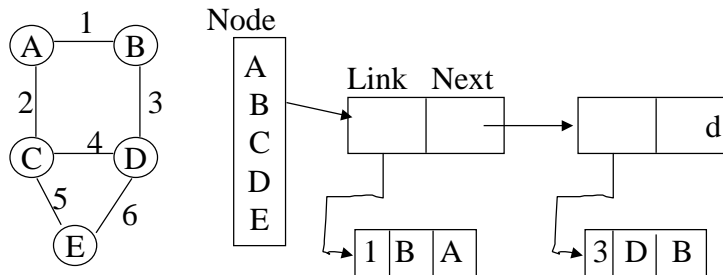
Incidence Matrix

For directed graphs +1 is  
source and -1 is sink of an arc

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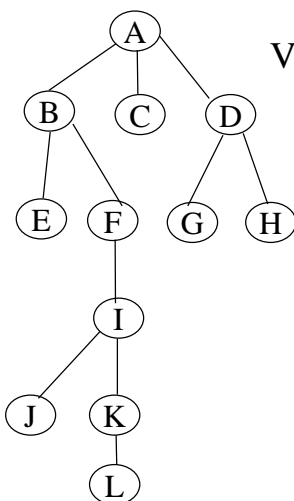
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For graph algorithms linked list presentation of adjacency is convenient



A Tree can be traversed by Breadth-first-search

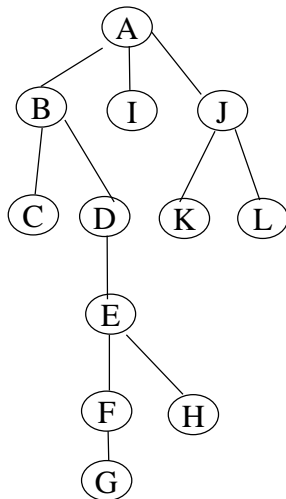
*Works for directed links*



```

Void <- BfsTree( n, root, n_adj_list )
dcl n_adj_list [n, list] /* array of lists of neighbors
scan_queue [queue]
InitializeQueue( scan_queue)
Enqueue(root, scan_queue)
while NotEmpty(scan_queue)
    node <- Dequeue(scan_queue)
    Visit (node)
    for each (neighbor, n_adj_list[node])
        Enqueue(neighbor, scan_queue)
    
```

## A Tree can also be traversed by Depth-first-search



*Works for directed links*

```
Void <- DfsTree( n, root, n_adj_list )
dcl n_adj_list [n, list]
```

```
Visit (root)
for each (neighbor, n_adj_list[node])
  DfsTree(n, neighbor, n_adj_list)
```

## An undirected graph can be traversed by Depth-first-search

```
Void <- Dfs ( n, root, n_adj_list )
  dcl n_adj_list [n, list]
  visited[n]      /* keeps track of progress
  {
    void <- DfsLoop(node)
      if not visited[node]
        visited[node] <- TRUE
        Visit (node)
        for each (neighbor, n_adj_list[node])
          DfsLoop(neighbor)
  }
  visited <- FALSE
  DfsLoop( root )
```

## We can now find and label the connected components of an arbitrary graph

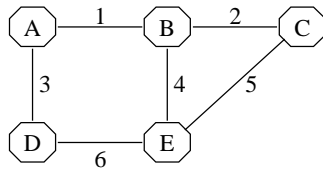
```
Void <- LabelComponents(n, n_adj_list)
dcl n_component_nr[n], n_adj_list[n, list]
void <- Visit(node)
    n_component_nr[node] <- ncomponents
n_component_nr <- 0
ncomponents <- 0
for each ( node, nodeset )
    if (n_component_nr[node] = 0
        ncomponents +=1
        Dfs( node, n_adj_list )
```

## Minimum Spanning Tree is the ST with minimum cost

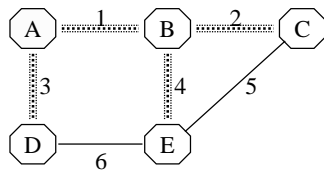
- We assign a length to each edge of the graph. “Length” can be distance, cost, a measure of delay or reliability.
- We look for minimum total length/cost, thus we talk about MST.
- If the graph is not connected, we may look for a minimum spanning forest.

$n = c + e$  , where  $n$  is the number of nodes,  $c$  the number of components and  $e$  number of edges selected so far holds always.

## MC to a *spanning tree* leads to reception only once in each node



- Requires on/off bit ( $\in$  ST) per link
- No group membership
- Concentrates traffic to the STlinks



- Ideal would be a tree that
  - spans the group members only
  - minimizes state information in nodes
  - optimizes routes based on metrics

## A Greedy MST algorithm

```
List <- Greedy( properties )
dcl properties [list, list],
      candidate_set[list], solution[list]

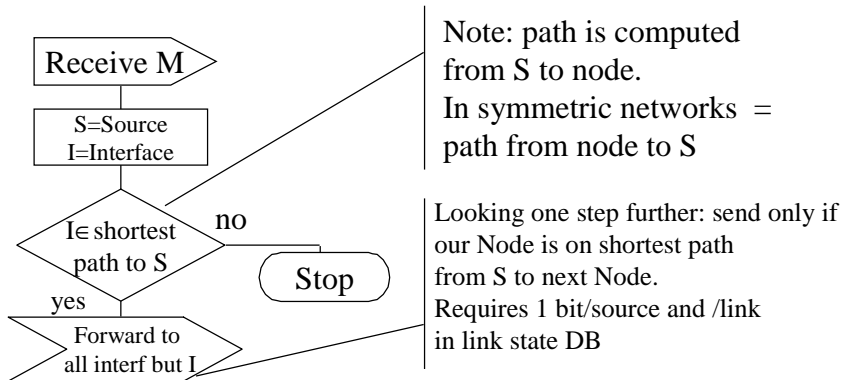
void <- GreedyLoop( *candidate_set, *solution)
dcl test_set[list], candidate_set[list], solution[list]

      element <- BestElementOf(candidate_set) /* for MST: shortest edge
      test_set <- element  $\cup$  solution
      If test_set is feasible /* for MST: no cycles
          solution <- test_set
      candidate_set <- candidate_set \ element
      If candidate set is not Empty
          Greedy_Loop( *candidate_set, *solution)

solution <-  $\emptyset$ 
If (candidate_set <- ElementsOf(properties)) is not Empty
    GreedyLoop( *candidate_set, *solution)
return(solution)
```

## Reverse-Path Forwarding computes an implicit spanning tree per source, is OK for dense trees

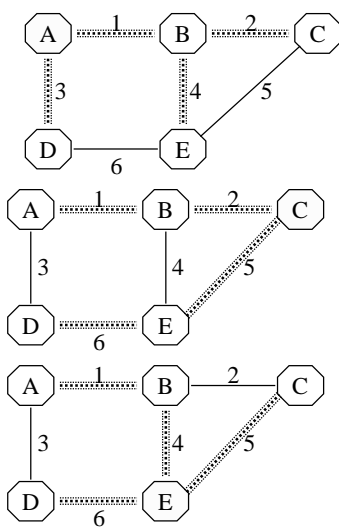
- RPF was first used in MBone



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## Reverse path forwarding properties

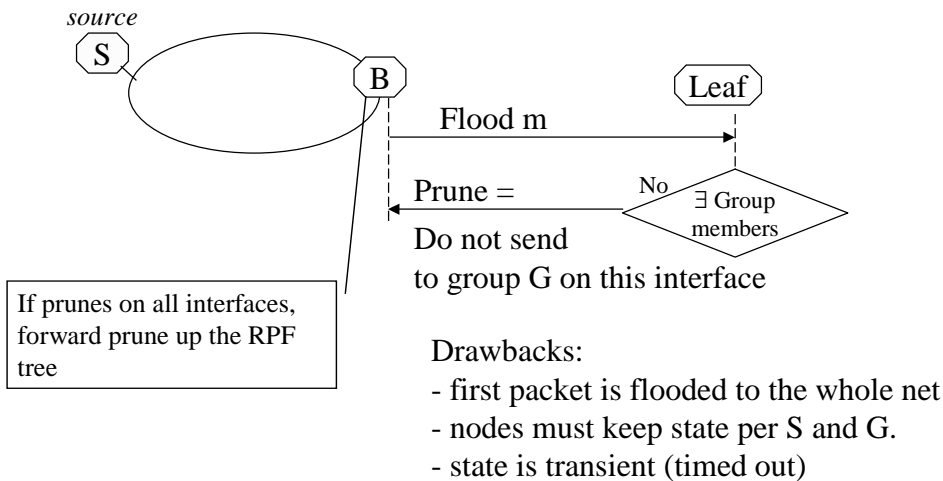


- No group membership but can be scoped by TTL
- Guarantees fastest possible delivery since uses shortest paths only
- Different tree for each source --> traffic is spread over multiple links leading to better network utilization

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## “Flood and prune” introduces dynamic group membership



## Steiner tree spans the group with the minimal cost according to link metrics

- Has never actually been used, only simulated:
  - Finding the minimum Steiner tree in a graph has exponential complexity and result is not necessarily optimal
  - The tree is undirected: links must be symmetrical
  - Algorithm is monolithic, can't be distributed
  - The tree is unstable when changes occur: traffic routes change dramatically when e.g a member leaves.
- Popular because of its mathematical complexity
- Leads to Center based approach (CBT, PIM)