NAME

Fmdn() - Virtual waiting time distribution function

IntFmdn() - Virtual waiting time distribution function for integral values of x

Mdn() – Calculates the state probabilities of a queue (queue length)

Fekdn() - Virtual waiting time distribution function

SYNOPSIS

#include <queuel.h>

double Fmdn(double x, double rho, int n);

double IntFmdn(int N, double rho, int n);

double *Mdn(double x, double rho, int n);

double Fekdn(double x, double rho, int k, int n);

DESCRIPTION

delim \$\$ These functions return the state probabilities or the virtual waiting time distribution of a M/D/n queue. (And the virtual waiting time distribution of a $E \sinh M/D/n$ queue.)

Fmdn() is a model for the M/D/n queuing system with Poisson arrivals and deterministic (constant) service time. Parameter x is the amount of unfinished work in the system. *Rho* is the load level of the system and n is the number of servers.

Fekdn() is a model for the $\{E \text{ sub } k\}/D/n$ queuing system with Erlang-k arrivals and deterministic (constant) service time. Parameter x is the amount of unfinished work in the system. *Rho* is the load level of the system and n is the number of servers.

ALGORITHM

\$M/D/n\$ waiting time distribution is calculated using the following algorithm (Iversen):

 $P_{\{W \le t\}} = sum from \{i=0\} to \{n-1\} sum from \{j=0\} to \{i\} P(j) sum from \{\{nu\}=0\} to \{T\} \{\{[A(\{nu\}-t)] sup \{\{nu\}n+\{nu\}-1-i\}\} over \{[\{nu\}n+n-1-i]!\}\} e sup \{A(\{nu\}-t)\},$

where P(j) is a state probability.

For integral values of the waiting time we have

 $P{\{w \le t\}} = sum from \{\{nu\}=0\} to \{n(t+1)-1\} P(\{nu\}).$

The state probabilities are calculated using the following procedure

- first we make an initial guess \$(M/M/n)\$:

- then we iterate until $\max \left\{ i \le I \right\}$ sup $\{(k)\}(i)$ -P sup $\{(k-1)\}(i)$ (i) ≤ 1

 $P \sup {(k)}(i)={\{sum from \{\{nu\}=0\} to \{n\} P \sup {(k-1)}(\{nu\})\}} P(i,h) + sum from {\{nu\}=n+1\} to {n+i} P \sup {(k-1)}(\{nu\}) P(n+i-{nu},h)}, si=0,1,...,I$

 $P \sup \{(k)\}(i)=P \sup \{(k)\}(i-1) \{\{lambda h\} over n\}$, i=I+1,...,I+n

 $SI = Sup \{(k)\} = Sup \{(k)\} = \{i=0\} \text{ to } \{I+n\} P \text{ sup } \{(k)\} = \{i=0\} \text{ to } \{I+n\} P \text{ sup } \{(k)\} = \{i=0\} \text{ to } \{I+n\} P \text{ sup } \{(k)\} = \{i=0\} \text{ to } \{i=0\} \text{$

 $P \sup \{(k)\}(i)=\{P \sup \{(k)\}(i)\} \text{ over } \{S \sup \{(k)\}\}, \ i=0,1,...,I+n\}$

 $(P(i,h) = \{ (\{lambda h\}) sup i\} over \{i!\} e sup \{ -(\{lambda h\}) \}$

\${E sub k}/D/n\$ waiting time distribution is calculated using the \$M/D/n\$ algorithm: \${E sub k}/D/r\$ (FIFO) is equivalent to \$M/D/r*k\$ (FIFO).

ERRORS

When \$ rho \$ is close to 1, these functions might give inaccurate results.

SEE ALSO

COST 224: Performance evaluation and design of multiservice networks