## NAME

Fmdn() - Virtual waiting time distribution function

IntFmdn() - Virtual waiting time distribution function for integral values of x

Mdn() – Calculates the state probabilities of a queue (queue length)

Fekdn() – Virtual waiting time distribution function

## SYNOPSIS

#include <queuel.h>

double Fmdn(double x, double rho, int n);

double IntFmdn(int N, double rho, int n);

double \*Mdn(double x, double rho, int n);

double Fekdn(double x, double rho, int k, int n);

#### DESCRIPTION

delim \$\$ These functions return the state probabilities or the virtual waiting time distribution of a M/D/n queue. (And the virtual waiting time distribution of a  $E \sinh M/D/n$  queue.)

**Fmdn**() is a model for the M/D/n queuing system with Poisson arrivals and deterministic (constant) service time. Parameter x is the amount of unfinished work in the system. *Rho* is the load level of the system and n is the number of servers.

**Fekdn**() is a model for the  $\{E \text{ sub } k\}/D/n$  queuing system with Erlang-k arrivals and deterministic (constant) service time. Parameter x is the amount of unfinished work in the system. *Rho* is the load level of the system and *n* is the number of servers.

#### ALGORITHM

\$M/D/n\$ waiting time distribution is calculated using the following algorithm (Iversen):

 $P_{s} = \sup \text{ from } \{i=0\} \text{ to } \{n-1\} \text{ sum from } \{j=0\} \text{ to } \{i\} P(j) \text{ sum from } \{nu\}=0\} \text{ to } \{T\} \{\{A(\{nu\}-t)\} \sup \{\{nu\}n+\{nu\}-1-i\}\} \text{ over } \{[\{nu\}n+n-1-i]\}\} \text{ e sup } \{A(\{nu\}-t)\},$ 

where P(j) is a state probability.

For integral values of the waiting time we have

 $P{\{w \le t\}} = sum from \{\{nu\}=0\} to \{n(t+1)-1\} P(\{nu\}).$ 

The state probabilities are calculated using the following procedure

- first we make an initial guess \$(M/M/n)\$:

- then we iterate until  $\max \left\{i \le I\right\}$  sup  $\{(k)\}(i)$ -P sup  $\{(k-1)\}(i)$  (i)  $\le (epsilon)$ :

 $P \sup \{(k)\}(i)=$   $f \sup \{(n_1)=0\}$  to  $\{n\} P \sup \{(k-1)\}(\{n_1\})$  P(i,h) + sum from  $\{(n_1)=0\}$  P(i,h) =

 $\{\{nu\}=n+1\}$  to  $\{n+i\}$  P sup  $\{(k-1)\}(\{nu\})$  P $(n+i-\{nu\},h)$ \$, i=0,1,...,I\$

 $P \sup {(k)}(i)=P \sup {(k)}(i-1) {\{lambda h\} over n}$ , i=I+1,...,I+n

 $S \sup \{(k)\} = \sup \text{ from } \{i=0\} \text{ to } \{I+n\} P \sup \{(k)\} (i)$ 

 $P \sup {(k)}(i)= P \sup {(k)}(i) \text{ sup } {(k)} \text{ sup } {(k)} \$ 

 $(P(i,h)=\{\{(\{lambda h\}) sup i\} over \{i!\}\} e sup \{-(\{lambda h\})\})$ 

\${E sub k}/D/n\$ waiting time distribution is calculated using the \$M/D/n\$ algorithm: \${E sub k}/D/r\$ (FIFO) is equivalent to \$M/D/r\*k\$ (FIFO).

### ERRORS

When \$ rho \$ is close to 1, these functions might give inaccurate results.

# SEE ALSO

COST 224: Performance evaluation and design of multiservice networks