



HELSINKI UNIVERSITY OF TECHNOLOGY
Department of Communications and Networking

Master's Thesis Presentation :

Forwarding Capacity of an Infinite Homogeneous Wireless Network

Jarno Nousiainen
25.2.2008

Supervisor: Professor Jorma Virtamo
Instructor: D.Sc.(Tech.) Pasi Lassila
Department of Communications and Networking

Outline

- ▣ Introduction
- ▣ Problem statement
 - Problem decomposition
- ▣ Network model
 - Performance measures
 - Network as a graph
- ▣ Max-flow min-cut theorem
- ▣ Moving window algorithm
- ▣ Results
- ▣ Conclusions

Introduction

■ Large network scenario

- Average distance between a source and a destination is much larger than the distance between adjacent nodes
- Paths consist of many hops and the intermediate nodes act as relays

■ Geographic routing

- Based on location information
- Nodes forward traffic towards the destination
- Routing around concave nodes
 - Concave nodes do not have neighbors in the direction of the destination

Problem statement

▣ Problem decomposition

- Macroscopic level corresponds to the distance between the source and destination nodes
- Microscopic level corresponds to the distance between neighboring nodes

▣ Macroscopic level routing

- Network nodes form a homogeneous, continuous medium
- Routes are smooth geometric curves

▣ Microscopic level forwarding

- Only the direction in which the packet is traversing is significant
- There exists a maximum flow a given MAC protocol can sustain
- The capacity can be shared between directions with time sharing

▣ Task: Find an upper bound for the maximal forwarding capacity

Routing:

- Define the geometric properties of the routes

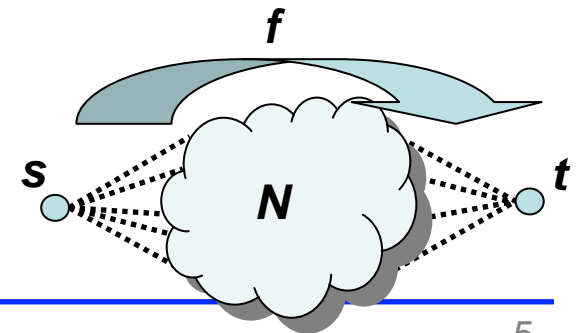
↓ *Direction of packet flow*

Forwarding:

- Maximize the packet flow in the given direction

Network model

- Nodes are distributed according to a homogeneous Poisson point process in two dimensions
 - Intensity λ
- Boolean interference model with a common, fixed transmission range R
 - Node can only receive a packet if it hears exactly one transmission
 - No separate interference range
 - Mean number of neighbors: $N_R = \lambda\pi R^2$
- Only relay traffic in single direction
 - Paths are long – mostly relay traffic anyway
 - Different directions by time sharing
- Slotted time



Performance measures

■ Single node's point of view

- Mean progress of a packet, D [m]
- $D = P(\text{node transmits}) \cdot P(\text{no collision} \mid \text{node transmits})$
 $\cdot E[\text{progress of a packet} \mid \text{successful transmission}]$
- Dimensionless measure: $u = \sqrt{\lambda} \cdot D$

■ Network level measure

- Mean density of progress, I [$1/(\text{m} \cdot \text{s})$]
- Total progress of packets per area per time
 - Also the number of packets crossing a line of unit length perpendicular to the direction of the packet flow in unit time

$$I = \frac{\lambda \cdot dA \cdot D}{dA \cdot \Delta t} = \frac{\sqrt{\lambda}}{\Delta t} \cdot u$$

Network as a graph

- Network is modeled as a flow network $N = (G, c, s, t)$
 - Nodes and links: $G = (V, E)$, link capacities: c , a source and a sink: s, t
- Schedule $\alpha = \{t_1, \dots, t_n\}$ assigns each transmission mode L_i with the proportion of time t_i it is used
 - Transmission mode is an independent set of links
 - Capacity of link e is the time share the link is active
- Flow f is a mapping $f : E \rightarrow \mathbb{R}^+$
 - $0 \leq f(e) \leq c(e)$ for all $e \in E$
 - Flows are preserved at every node (except at the source and the sink)
 - Value of a flow $w(f)$ is the net flow leaving the source (or entering the sink)
- Cut $q = (S, T)$ of N is a partition $V = S + T$ ($V = S \cup T, S \cap T = \emptyset$)
 - Capacity of a cut is a sum of the capacities of crossing links

$$c(e) = \sum_{i=1}^n t_i 1_{\{e \in L_i\}}$$

Max-flow min-cut theorem

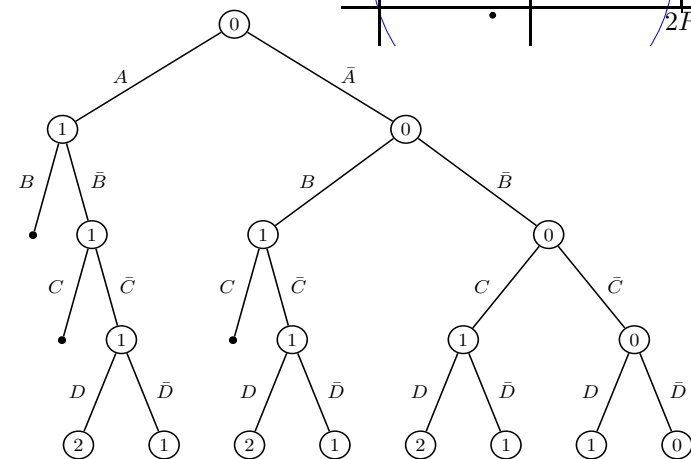
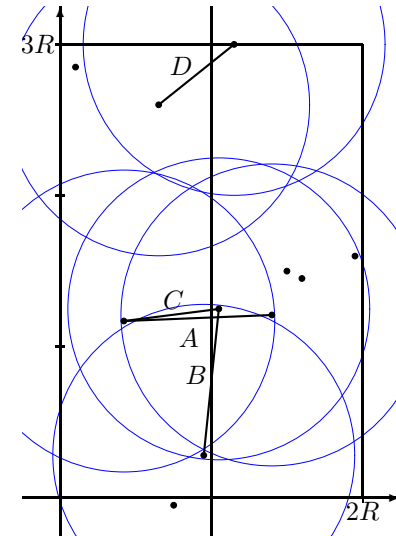
- ▣ (Ford and Fulkerson 1956) The maximal value of a flow on a flow network N equals the minimal capacity of a cut in N .
- ▣ In a wireless case, we have to find the optimal transmission radius and schedule as well
- ▣ We get an upper bound for the capacity by examining a smaller set of cuts

$$\max_R \max_{\alpha} \min_{q \in Q} c(q, \alpha; R)$$

$$\begin{aligned} w(f_R^*) &= \max_{\alpha} \min_{q \in Q} c(q, \alpha) \\ &\leq \max_{\alpha} \min_{q \in Q' \subset Q} c(q, \alpha) \end{aligned}$$

Moving window algorithm

- Let Q' consist of one arbitrary cut corresponding to a straight line perpendicular to the direction of the packet flow
 - Maximizing with respect to α finds the size of the maximum independent set
- Window separating the links above and below is moved along the line
 - Maximum is found recursively by solving the maximum so far given a combination of active links in the window
 - Leaves of a binary tree represent the possible link combinations and the value assigned to each leaf corresponds to the optimum value

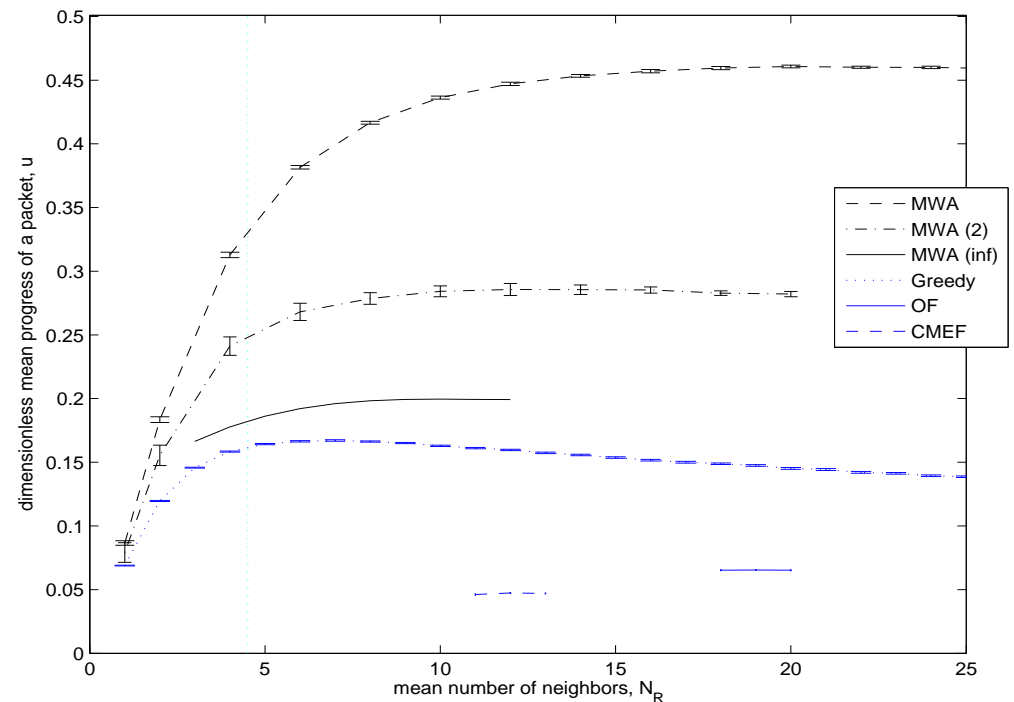


MWA – remarks

- Length of the simulation is not limited
 - The result converges unbiasedly towards the true value
- Capacity of one cut can only be achieved very locally
 - There is no horizontal interference
- We get a tighter upper bound by increasing the number of cuts in Q'
- Two cuts:
 - We want to find the distance with maximum interference
- Infinite number of cuts:
 - Number of crossed cuts is proportional to the progress of the link
 - Opposite sides of the window are connected together to form a tube
 - The result is still an upper bound, since the corresponding flow network is not connected
 - Gives the maximum capacity in one time slot

Results

- The results for one, two, and infinite number of cuts
- Greedy methods approximates the case with infinite number of cuts
- OF and CMEF are feasible forwarding methods
 - Actual methods give a lower bound for the maximum capacity
 - Opportunistic forwarding (OF) represents what can be achieved through local coordination



Conclusions

- Large, dense ad hoc network
 - Problem decomposition: Macroscopic (end-to-end) vs. microscopic (adjacent nodes)
 - Poisson Boolean model
 - Maximal forwarding capacity characteristic to the medium

- Augmented Max-flow min-cut theorem
 - Upper bound by examining a limited set of cuts

- The tightest upper bound is still three times the highest achieved dimensionless mean progress