

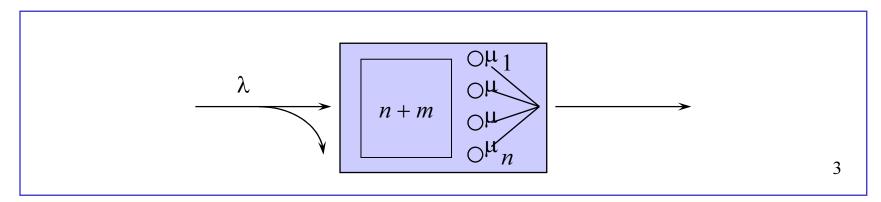
7. Loss systems

Contents

- Refresher: Simple teletraffic model
- Poisson model (∞ customers, ∞ servers)
- Application to flow level modelling of streaming data traffic
- Erlang model (∞ customers, $n < \infty$ servers)
- Application to telephone traffic modelling in trunk network
- Binomial model ($k < \infty$ customers, n = k servers)
- Engset model ($k < \infty$ customers, n < k servers)
- Application to telephone traffic modelling in access network

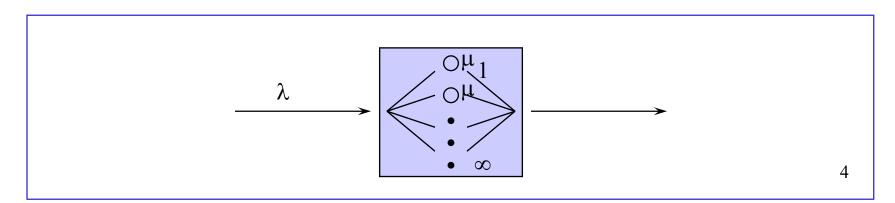
Simple teletraffic model

- Customers arrive at rate λ (customers per time unit)
 - $-1/\lambda$ = average inter-arrival time
- Customers are served by n parallel servers
- When busy, a server serves at rate μ (customers per time unit)
 - $-1/\mu$ = average service time of a customer
- There are n + m customer places in the system
 - at least n service places and at most m waiting places
- It is assumed that blocked customers (arriving in a full system) are lost



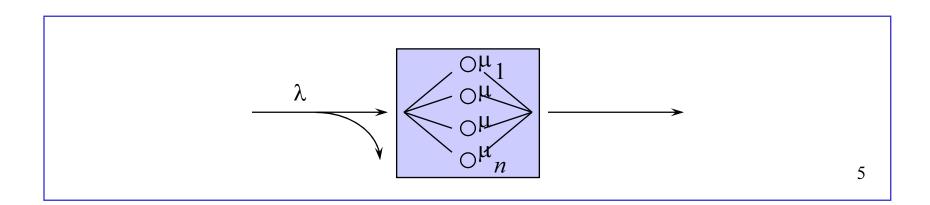
Infinite system

- Infinite number of servers $(n = \infty)$, no waiting places (m = 0)
 - No customers are lost or even have to wait before getting served
- Sometimes,
 - this hypothetical model can be used to get some approximate results for a real system (with finite system capacity)
- Always,
 - it gives bounds for the performance of a real system (with finite system capacity)
 - it is much easier to analyze than the corresponding finite capacity models



Pure loss system

- Finite number of servers $(n < \infty)$, n service places, no waiting places (m = 0)
 - If the system is full (with all n servers occupied) when a customer arrives,
 it is not served at all but lost
 - Some customers may be lost
- From the customer's point of view, it is interesting to know e.g.
 - What is the probability that the system is full when it arrives?



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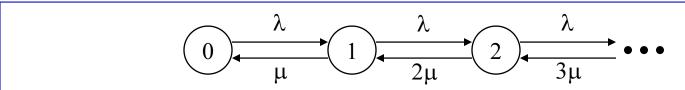
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Poisson model ($M/M/\infty$)

- Definition: Poisson model is the following simple teletraffic model:
 - Infinite number of independent customers $(k = \infty)$
 - Interarrival times are IID and exponentially distributed with mean $1/\lambda$
 - so, customers arrive according to a Poisson process with intensity λ
 - **Infinite** number of servers $(n = \infty)$
 - Service times are IID and exponentially distributed with mean $1/\mu$
 - No waiting places (m = 0)
- Poisson model:
 - Using Kendall's notation, this is an $M/M/\infty$ queue
 - Infinite system, and, thus, lossless
- Notation:
 - $a = \lambda/\mu = \text{traffic intensity}$

State transition diagram

- Let *X*(*t*) denote the number of customers in the system at time *t*
 - Assume that X(t) = i at some time t, and consider what happens during a short time interval (t, t+h]:
 - with prob. $\lambda h + o(h)$, a new customer arrives (state transition $i \rightarrow i+1$)
 - if i > 0, then, with prob. $i\mu h + o(h)$, a customer leaves the system (state transition $i \to i-1$)
- Process X(t) is clearly a Markov process with state transition diagram



• Note that process X(t) is an irreducible birth-death process with an infinite state space $S = \{0,1,2,...\}$

Equilibrium distribution (1)

Local balance equations (LBE):

$$\pi_{i}\lambda = \pi_{i+1}(i+1)\mu$$

$$\Rightarrow \pi_{i+1} = \frac{\lambda}{(i+1)\mu}\pi_{i} = \frac{a}{i+1}\pi_{i}$$

$$\Rightarrow \pi_{i} = \frac{a^{i}}{i!}\pi_{0}, \quad i = 0,1,2,...$$
(LBE)

Normalizing condition (N):

$$\sum_{i=0}^{\infty} \pi_i = \pi_0 \sum_{i=0}^{\infty} \frac{a^i}{i!} = 1$$

$$\Rightarrow \pi_0 = \left(\sum_{i=0}^{\infty} \frac{a^i}{i!}\right)^{-1} = \left(e^a\right)^{-1} = e^{-a}$$

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Equilibrium distribution (2)

Thus, the equilibrium distribution is a Poisson distribution:

$$X \sim \text{Poisson}(a)$$

 $P\{X = i\} = \pi_i = \frac{a^i}{i!}e^{-a}, \quad i = 0,1,2,...$
 $E[X] = a, \quad D^2[X] = a$

- Remark: Insensitivity with respect to service time distribution
 - The result is **insensitive** to the service time distribution, that is: it is valid for **any** service time distribution with mean $1/\mu$
 - So, instead of the M/M/∞ model,
 we can consider, as well, the more general M/G/∞ model

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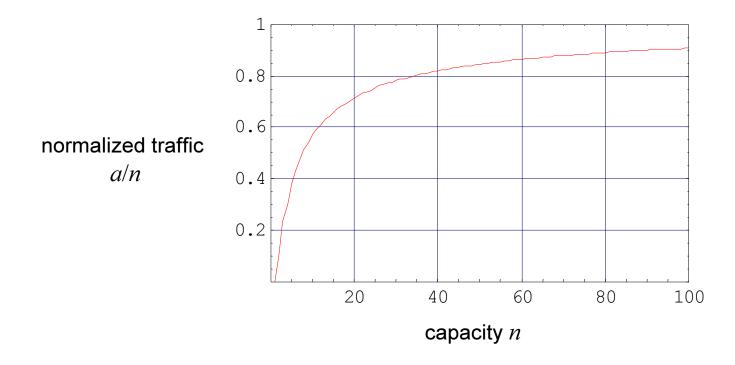
Application to flow level modelling of streaming data traffic

- Poisson model may be applied to flow level modelling of streaming data traffic
 - customer = UDP flow with constant bit rate (CBR)
 - $-\lambda$ = flow arrival rate (flows per time unit)
 - $h = 1/\mu$ = average flow duration (time units)
 - $a = \lambda/\mu$ = traffic intensity
 - r = bit rate of a flow (data units per time unit)
 - N = nr of active flows obeying Poisson(a) distribution
- When the total transmission rate Nr exceeds the link capacity C = nr, bits are lost
 - loss ratio $p_{\rm loss}$ gives the ratio between the traffic lost and the traffic offered:

$$p_{\text{loss}} = \frac{E[(Nr - C)^{+}]}{E[Nr]} = \frac{E[(N - n)^{+}]}{E[N]} = \frac{1}{a} \sum_{i=n+1}^{\infty} (i - n) \frac{a^{i}}{i!} e^{-a}$$
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Multiplexing gain

- We determine traffic intensity a so that loss ratio $p_{\rm loss} < 1\%$
- **Multiplexing gain** is described by the traffic intensity per capacity unit, a/n, as a function of capacity n



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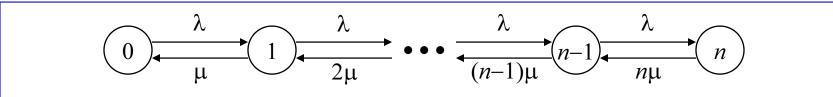
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Erlang model (M/M/n/n)

- **Definition**: **Erlang model** is the following simple teletraffic model:
 - Infinite number of independent customers $(k = \infty)$
 - Interarrival times are IID and exponentially distributed with mean $1/\lambda$
 - so, customers arrive according to a Poisson process with intensity λ
 - **Finite** number of servers (n < ∞)
 - Service times are IID and exponentially distributed with mean $1/\mu$
 - No waiting places (m = 0)
- Erlang model:
 - Using Kendall's notation, this is an M/M/n/n queue
 - Pure loss system, and, thus, lossy
- Notation:
 - $a = \lambda/\mu = \text{traffic intensity}$

State transition diagram

- Let *X*(*t*) denote the number of customers in the system at time *t*
 - Assume that X(t) = i at some time t, and consider what happens during a short time interval (t, t+h]:
 - with prob. $\lambda h + o(h)$, a new customer arrives (state transition $i \rightarrow i+1$)
 - with prob. $i\mu h + o(h)$, a customer leaves the system (state transition $i \rightarrow i-1$)
- Process X(t) is clearly a Markov process with state transition diagram



• Note that process X(t) is an irreducible birth-death process with a finite state space $S = \{0,1,2,...,n\}$

Equilibrium distribution (1)

Local balance equations (LBE):

$$\pi_{i}\lambda = \pi_{i+1}(i+1)\mu$$
 (LBE)

$$\Rightarrow \pi_{i+1} = \frac{\lambda}{(i+1)\mu}\pi_{i} = \frac{a}{i+1}\pi_{i}$$

$$\Rightarrow \pi_{i} = \frac{a^{i}}{i!}\pi_{0}, \quad i = 0,1,...,n$$

Normalizing condition (N):

$$\sum_{i=0}^{n} \pi_i = \pi_0 \sum_{i=0}^{n} \frac{a^i}{i!} = 1$$

$$\Rightarrow \pi_0 = \left(\sum_{i=0}^{n} \frac{a^i}{i!}\right)^{-1}$$

$$\Rightarrow \pi_0 = \left(\sum_{i=0}^{n} \frac{a^i}{i!}\right)^{-1}$$

Equilibrium distribution (2)

• Thus, the equilibrium distribution is a **truncated Poisson distribution**:

$$P\{X = i\} = \pi_i = \frac{\frac{a^i}{i!}}{\sum_{j=0}^{n} \frac{a^j}{j!}}, \quad i = 0, 1, \dots, n$$

- Remark: Insensitivity with respect to the service time distribution
 - The result is **insensitive** to the service time distribution, that is: it is valid for **any** service time distribution with mean $1/\mu$
 - So, instead of the M/M/n/n model, we can consider, as well, the more general M/G/n/n model

Time blocking

- **Time blocking** B_t = probability that all n servers are occupied at an arbitrary time = the fraction of time that all n servers are occupied
- For a stationary Markov process, this equals the probability π_n of the equilibrium distribution π . Thus,

$$B_t := P\{X = n\} = \pi_n = \frac{\frac{\underline{a}^n}{n!}}{\sum_{j=0}^n \frac{\underline{a}^j}{j!}}$$

Call blocking

- Call blocking B_c = probability that an arriving customer finds all n servers occupied = the fraction of arriving customers that are lost
- However, due to Poisson arrivals and PASTA property, the probability that an arriving customer finds all n servers occupied equals the probability that all n servers are occupied at an arbitrary time,
- In other words, call blocking $B_{\rm c}$ equals time blocking $B_{\rm t}$:

$$B_{c} = B_{t} = \frac{\frac{a^{n}}{n!}}{\sum_{j=0}^{n} \frac{a^{j}}{j!}}$$

This is Erlang's blocking formula

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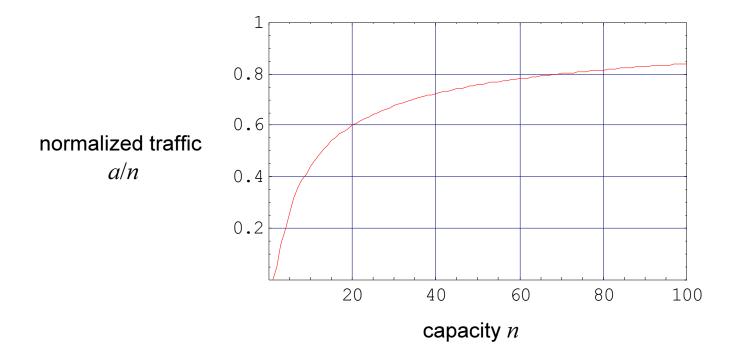
Application to telephone traffic modelling in trunk network

- Erlang model may be applied to modelling of telephone traffic in trunk network where the number of potential users of a link is large
 - customer = call
 - $-\lambda$ = call arrival rate (calls per time unit)
 - $h = 1/\mu$ = average call holding time (time units)
 - $a = \lambda/\mu$ = traffic intensity
 - n = link capacity (channels)
- A call is lost if all n channels are occupied when the call arrives
 - call blocking B_c gives the probability of such an event

$$B_{c} = \frac{\frac{a^{n}}{n!}}{\sum_{j=0}^{n} \frac{a^{j}}{j!}}$$

Multiplexing gain

- We determine traffic intensity a so that call blocking $B_{\rm c} < 1\%$
- Multiplexing gain is described by the traffic intensity per capacity unit, a/n, as a function of capacity n



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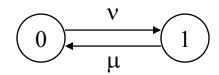
Binomial model (M/M/k/k/k)

- **Definition**: **Binomial model** is the following (simple) teletraffic model:
 - **Finite** number of independent customers $(k < \infty)$
 - on-off type customers (alternating between idleness and activity)
 - Idle times are IID and exponentially distributed with mean 1/v
 - As many servers as customers (n = k)
 - Service times are IID and exponentially distributed with mean $1/\mu$
 - No waiting places (m=0)
- Binomial model:
 - Using Kendall's notation, this is an M/M/k/k/k queue
 - Although a finite system, this is clearly lossless
- On-off type customer:



On-off type customer (1)

- Let $X_j(t)$ denote the state of customer j (j = 1,2,...,k) at time t
 - State 0 = idle, state 1 = active = in service
 - Consider what happens during a short time interval (t, t+h]:
 - if $X_j(t) = 0$, then, with prob. vh + o(h), the customer becomes active (state transition $0 \to 1$)
 - if $X_j(t) = 1$, then, with prob. $\mu h + o(h)$, the customer becomes idle (state transition $1 \to 0$)
- Process $X_i(t)$ is clearly a Markov process with state transition diagram



• Note that process $X_j(t)$ is an irreducible birth-death process with a finite state space $S = \{0,1\}$

On-off type customer (2)

Local balance equations (LBE):

$$\pi_0^{(j)} \nu = \pi_1^{(j)} \mu \implies \pi_1^{(j)} = \frac{\nu}{\mu} \pi_0^{(j)}$$

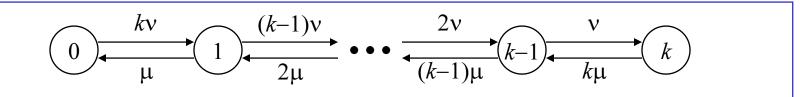
Normalizing condition (N):

$$\pi_0^{(j)} + \pi_1^{(j)} = \pi_0^{(j)} (1 + \frac{\nu}{\mu}) = 1 \implies \pi_0^{(j)} = \frac{\mu}{\nu + \mu}, \quad \pi_1^{(j)} = \frac{\nu}{\nu + \mu}$$

- So, the equilibrium distribution of a single customer is the **Bernoulli** distribution with success probability $v/(v+\mu)$
 - offered traffic is $v/(v+\mu)$
- From this, we could deduce that the equilibrium distribution of the state of the whole system (that is: the number of active customers) is the binomial distribution $Bin(k, \nu/(\nu+\mu))$

State transition diagram

- Let X(t) denote the number of active customers
 - Assume that X(t) = i at some time t, and consider what happens during a short time interval (t, t+h]:
 - if i < k, then, with prob. (k-i)vh + o(h), an idle customer becomes active (state transition $i \rightarrow i+1$)
 - if i > 0, then, with prob. $i\mu h + o(h)$, an active customer becomes idle (state transition $i \rightarrow i-1$)
- Process X(t) is clearly a Markov process with state transition diagram



• Note that process X(t) is an irreducible birth-death process with a finite state space $S = \{0,1,...,k\}$

Equilibrium distribution (1)

Local balance equations (LBE):

$$\pi_{i}(k-i)\nu = \pi_{i+1}(i+1)\mu$$
 (LBE)
$$\Rightarrow \pi_{i+1} = \frac{(k-i)\nu}{(i+1)\mu}\pi_{i}$$

$$\Rightarrow \pi_{i} = \frac{k!}{i!(k-i)!}(\frac{\nu}{\mu})^{i}\pi_{0} = {k \choose i}(\frac{\nu}{\mu})^{i}\pi_{0}, \quad i = 0,1,...,k$$

Normalizing condition (N):

$$\sum_{i=0}^{k} \pi_{i} = \pi_{0} \sum_{i=0}^{k} {k \choose i} (\frac{\nu}{\mu})^{i} = 1$$

$$\Rightarrow \pi_{0} = \left(\sum_{i=0}^{k} {k \choose i} (\frac{\nu}{\mu})^{i}\right)^{-1} = (1 + \frac{\nu}{\mu})^{-k} = (\frac{\mu}{\nu + \mu})^{k}_{29}$$

Equilibrium distribution (2)

Thus, the equilibrium distribution is a binomial distribution:

$$X \sim \text{Bin}(k, \frac{\nu}{\nu + \mu})$$

$$P\{X = i\} = \pi_i = {k \choose i} \left(\frac{\nu}{\nu + \mu}\right)^i \left(\frac{\mu}{\nu + \mu}\right)^{k - i}, \quad i = 0, 1, ..., k$$

$$E[X] = \frac{k\nu}{\nu + \mu}, \quad D^2[X] = k \cdot \frac{\nu}{\nu + \mu} \cdot \frac{\mu}{\nu + \mu} = \frac{k\nu\mu}{(\nu + \mu)^2}$$

- Remark: Insensitivity w.r.t. service time and idle time distribution
 - The result is **insensitive both** to the service **and** the idle time distribution, that is: it is valid for **any** service time distribution with mean $1/\nu$ and **any** idle time distribution with mean $1/\nu$
 - So, instead of the M/M/k/k model, we can consider, as well, the more general G/G/k/k/k model

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Engset model (M/M/n/n/k)

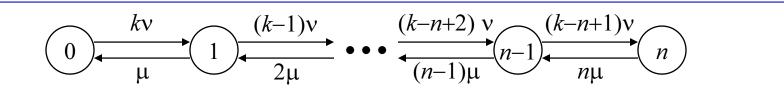
- **Definition**: **Engset model** is the following (simple) teletraffic model:
 - **Finite** number of independent customers $(k < \infty)$
 - on-off type customers (alternating between idleness and activity)
 - Idle times are IID and exponentially distributed with mean 1/v
 - Less servers than customers (n < k)
 - Service times are IID and exponentially distributed with mean $1/\mu$
 - No waiting places (m = 0)
- Engset model:
 - Using Kendall's notation, this is an M/M/n/n/k queue
 - This is a pure loss system, and, thus, lossy
- On-off type customer:

Note: If the system is full when an idle cust. tries to become an active cust., a new idle period starts.

| 1 idleness | ce | blocking! idle idle | |
|------------|----|------------------------|--|
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State transition diagram

- Let X(t) denote the number of active customers
 - Assume that X(t) = i at some time t, and consider what happens during a short time interval (t, t+h]:
 - if i < n, then, with prob. (k-i)vh + o(h), an idle customer becomes active (state transition $i \rightarrow i+1$)
 - if i > 0, then, with prob. $i\mu h + o(h)$, an active customer becomes idle (state transition $i \rightarrow i-1$)
- Process X(t) is clearly a Markov process with state transition diagram



• Note that process X(t) is an irreducible birth-death process with a finite state space $S = \{0,1,...,n\}$

Equilibrium distribution (1)

Local balance equations (LBE):

$$\pi_{i}(k-i)\nu = \pi_{i+1}(i+1)\mu$$
 (LBE)
$$\Rightarrow \pi_{i+1} = \frac{(k-i)\nu}{(i+1)\mu}\pi_{i}$$

$$\Rightarrow \pi_{i} = \frac{k!}{i!(k-i)!}(\frac{\nu}{\mu})^{i}\pi_{0} = {k \choose i}(\frac{\nu}{\mu})^{i}\pi_{0}, \quad i = 0,1,...,n$$

Normalizing condition (N):

$$\sum_{i=0}^{n} \pi_i = \pi_0 \sum_{i=0}^{n} {k \choose i} \left(\frac{\nu}{\mu}\right)^i = 1$$

$$\Rightarrow \pi_0 = \left(\sum_{i=0}^{n} {k \choose i} \left(\frac{\nu}{\mu}\right)^i\right)^{-1}$$
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Equilibrium distribution (2)

Thus, the equilibrium distribution is a truncated binomial distribution:

$$P\{X=i\} = \pi_i = \frac{\binom{k}{i}\binom{\nu}{\mu}^i}{\sum\limits_{j=0}^{n}\binom{k}{j}\binom{\nu}{\mu}^j} = \frac{\binom{k}{i}\binom{\nu}{\nu+\mu}^i\binom{\nu}{\nu+\mu}^i\binom{\mu}{\nu+\mu}^{k-i}}{\sum\limits_{j=0}^{n}\binom{k}{j}\binom{\nu}{\nu+\mu}^j\binom{\nu}{\nu+\mu}^j\binom{\mu}{\nu+\mu}^{k-j}}, i=0,\dots,n$$

- Offered traffic is $kv/(v+\mu)$
- Remark: Insensitivity w.r.t. service time and idle time distribution
 - The result is **insensitive both** to the service **and** the idle time distribution, that is: it is valid for **any** service time distribution with mean $1/\nu$ idle time distribution with mean $1/\nu$
 - So, instead of the M/M/n/n/k model, we can consider, as well, the more general G/G/n/n/k model

Time blocking

- **Time blocking** B_t = probability that all n servers are occupied at an arbitrary time = the fraction of time that all n servers are occupied
- For a stationary Markov process, this equals the probability π_n of the equilibrium distribution π . Thus,

$$B_{\mathsf{t}} := P\{X = n\} = \pi_n = \frac{\binom{k}{n} \left(\frac{\nu}{\mu}\right)^n}{\sum_{j=0}^{n} \binom{k}{j} \left(\frac{\nu}{\mu}\right)^j}$$

Call blocking (1)

- Call blocking B_c = probability that an arriving customer finds all n servers occupied = the fraction of arriving customers that are lost
 - In the Engset model, however, the "arrivals" do not follow a Poisson process. Thus, we cannot utilize the PASTA property any more.
 - In fact, the distribution of the state that an "arriving" customer sees differs from the equilibrium distribution. Thus, call blocking $B_{\rm c}$ does **not** equal time blocking $B_{\rm t}$ in the Engset model.

Call blocking (2)

- Let π_i^* denote the probability that there are i active customers when an idle customer becomes active (which is called an "arrival")
- Consider a long time interval (0,T):
 - During this interval, the average time spent in state i is $\pi_i T$
 - During this time, the average number of "arriving" customers (who all see the system to be in state i) is $(k-i)v \cdot \pi_i T$
 - During the whole interval, the average number of "arriving" customers is $\sum_j (k\!-\!j) \mathbf{v} \cdot \mathbf{\pi}_j T$
- Thus,

$$\pi_{i}^{*} = \frac{(k-i)\nu \cdot \pi_{i}T}{\sum_{j=0}^{n} (k-j)\nu \cdot \pi_{j}T} = \frac{(k-i)\cdot \pi_{i}}{\sum_{j=0}^{n} (k-j)\cdot \pi_{j}}, \quad i = 0,1,...,n$$

Call blocking (3)

It can be shown (exercise!) that

$$\pi_{i}^{*} = \frac{\binom{k-1}{i} (\frac{\nu}{\mu})^{i}}{\sum_{j=0}^{n} \binom{k-1}{j} (\frac{\nu}{\mu})^{j}}, \quad i = 0, 1, \dots, n$$

 If we write explicitly the dependence of these probabilities on the total number of customers, we get the following result:

$$\pi_i * (k) = \pi_i (k-1), i = 0,1,...,n$$

In other words, an "arriving" customer sees such a system where there
is one customer less (itself!) in equilibrium

Call blocking (4)

• By choosing i = n, we get the following formula for the call blocking probability:

$$B_{c}(k) = \pi_{n} * (k) = \pi_{n}(k-1) = B_{t}(k-1)$$

• Thus, for the Engset model, the call blocking in a system with k customers equals the time blocking in a system with k-1 customers:

$$B_{c}(k) = B_{t}(k-1) = \frac{\binom{k-1}{n} (\frac{\nu}{\mu})^{n}}{\sum_{j=0}^{n} \binom{k-1}{j} (\frac{\nu}{\mu})^{j}}$$

This is Engset's blocking formula

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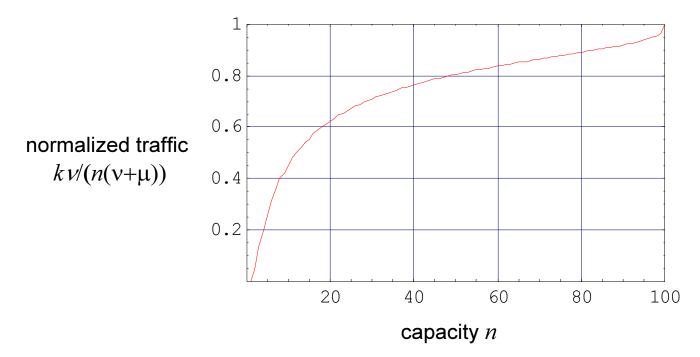
Application to telephone traffic modelling in access network

- Engset model may be applied to modelling of telephone traffic in access network where the nr of potential users of a link is moderate
 - customer = call
 - v = call arrival rate per idle user (calls per time unit)
 - $1/\mu$ = average call holding time (time units)
 - k = number of potential users
 - n = link capacity (channels)
- A call is lost if all n channels are occupied when the call arrives
 - call blocking B_c gives the probability of such an event

$$B_{c} = \frac{\binom{k-1}{n} (\frac{\nu}{\mu})^{n}}{\sum_{j=0}^{n} \binom{k-1}{j} (\frac{\nu}{\mu})^{j}}$$

Multiplexing gain

- We assume that an access link is loaded by k = 100 potential users
- We determine traffic intensity $k\nu/(\nu+\mu)$ so that call blocking $B_{\rm c} < 1\%$
- Multiplexing gain is described by the traffic intensity per capacity unit, $kv/(n(v+\mu))$, as a function of capacity n



THE END

