



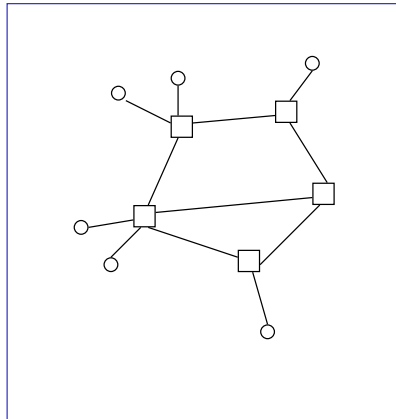
1. Introduction

Contents

- Telecommunication networks and switching modes
- Purpose of Teletraffic Theory
- Teletraffic models
- Little's formula

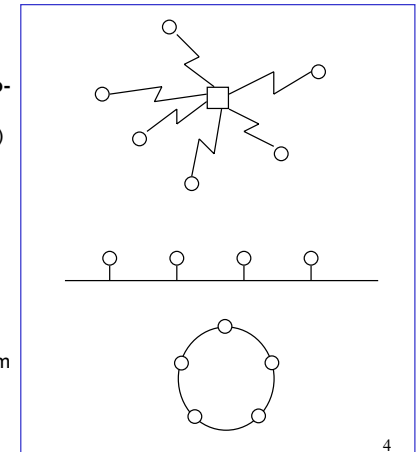
Telecommunication network

- A simple model of a telecommunication network consists of
 - **nodes**
 - terminals 
 - network nodes 
 - **links** between nodes
- **Access network**
 - connects the terminals to the network nodes
- **Trunk network**
 - connects the network nodes to each other



Shared medium as an access network

- In the previous model,
 - connections between terminals and network nodes are **point-to-point** type (\Rightarrow no resource sharing within the access netw.)
- In some cases, such as
 - mobile telephone network
 - local area network (LAN) connecting computers
 the access network consists of **shared medium**:
 - users have to **compete** for the resources of this shared medium
 - **multiple access (MA)** techniques are needed

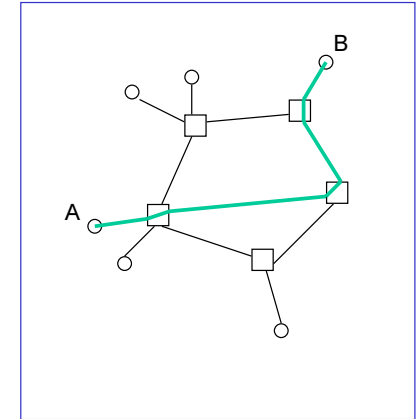


Switching modes

- **Circuit switching**
 - telephone networks
 - mobile telephone networks
 - optical networks
- **Packet switching**
 - data networks
 - two possibilities
 - **connection oriented:** e.g. X.25, Frame Relay
 - **connectionless:** e.g. Internet (IP), SS7 (MTP)
- **Cell switching**
 - ATM networks
 - connection oriented
 - fast packet switching with fixed length packets (cells)

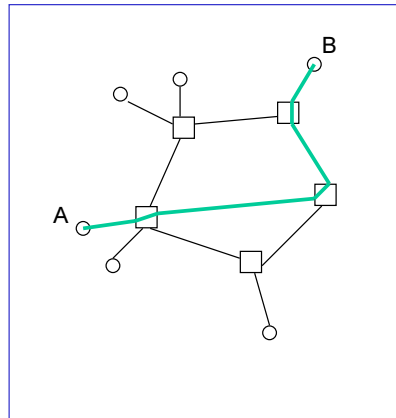
Circuit switching (1)

- **Connection oriented:**
 - connections **set up** end-to-end before information transfer
 - resources **reserved** for the whole duration of connection
 - if resources are not available, the call is blocked and lost
- Information transfer as **continuous stream**



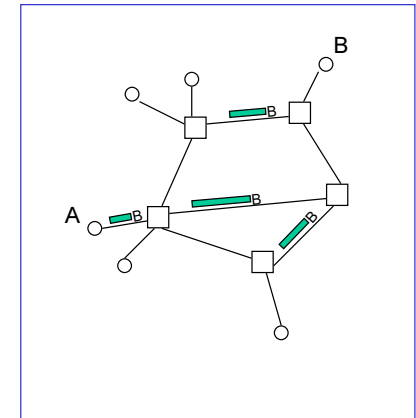
Circuit switching (2)

- Before information transfer
 - Set-up delay
- During information transfer
 - signal propagation delay
 - no overhead
 - no extra delays
- Example: telephone network



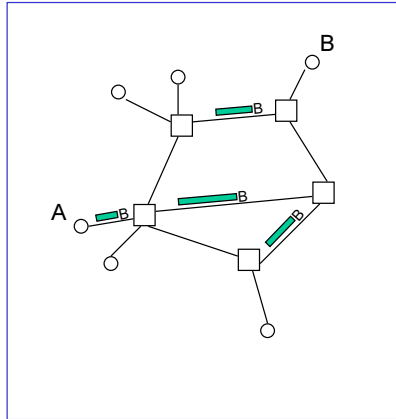
Connectionless packet switching (1)

- **Connectionless:**
 - no connection set-up
 - no resource reservation
 - no blocking
- Information transfer as **discrete packets**
 - varying length
 - global address (of the destination)



Connectionless packet switching (2)

- Before information transfer
 - no delays
- During information transfer
 - overhead (header bytes)
 - packet processing delays
 - queueing delays (since packets compete for joint resources)
 - transmission delays (due to finite capacity links)
 - signal propagation delay
 - packet losses (due to finite buffers)
- Example: Internet (IP-layer)

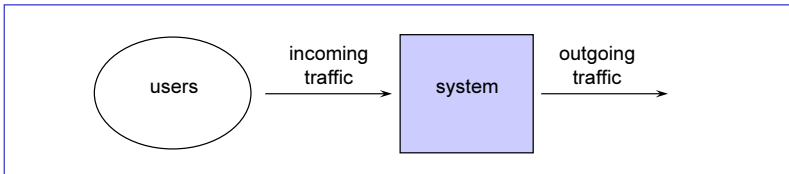


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Traffic point of view

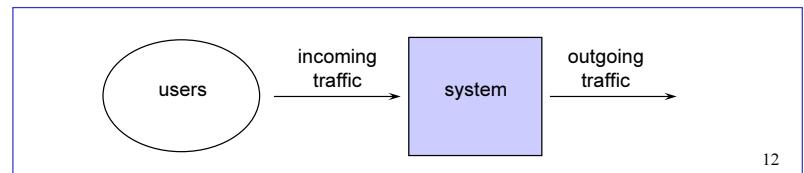
- Telecommunication system from the **traffic point of view**:



- Ideas:
 - the **system serves** the incoming **traffic**
 - the traffic is generated by the **users** of the system

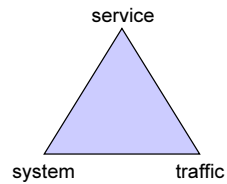
Interesting questions

- Given the system and incoming traffic, what is the quality of service experienced by the user?
- Given the incoming traffic and required quality of service, how should the system be dimensioned?
- Given the system and required quality of service, what is the maximum traffic load?



General purpose (1)

- Determine **relationships** between the following three factors:
 - **quality of service**
 - **traffic load**
 - **system capacity**

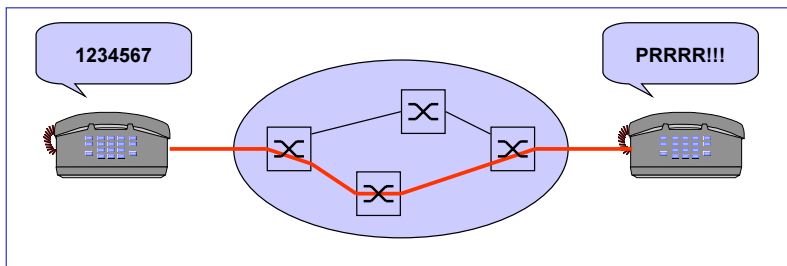


General purpose (2)

- System can be
 - a single device (e.g. link between two telephone exchanges, link in an IP network, packet processor in a data network, router's transmission buffer, or statistical multiplexer in an ATM network)
 - the whole network (e.g. telephone or data network) or some part of it
- Traffic consists of
 - bits, packets, bursts, flows, connections, calls, ...
 - depending on the system and time scale considered
- Quality of service can be described from the point of view of
 - the customer (e.g. call blocking, packet loss, packet delay, or throughput)
 - the system, in which case we use the term **performance** (e.g. processor or link utilization, or maximum network load)

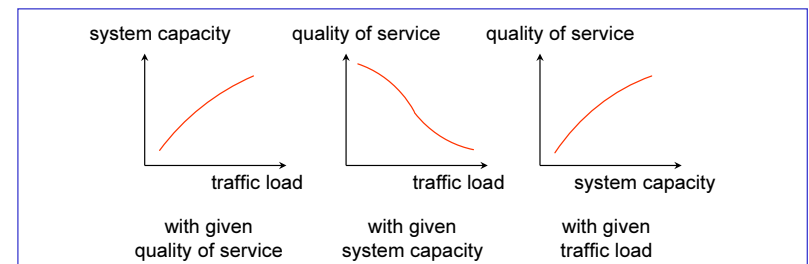
Example

- Telephone call
 - traffic = telephone calls by everybody
 - system = telephone network
 - quality of service = probability that the phone rings at the destination



Relationships between the three factors

- **Qualitatively**, the relationships are as follows:



- To describe the relationships **quantitatively**, **mathematical models** are needed

Teletraffic models

- Teletraffic models are **stochastic** (= **probabilistic**)
 - systems themselves are usually deterministic but traffic is typically stochastic
 - “you never know, who calls you and when”
- It follows that the variables in these models are **random variables**, e.g.
 - number of ongoing calls
 - number of packets in a buffer
- Random variable is described by its **distribution**, e.g.
 - probability that there are n ongoing calls
 - probability that there are n packets in the buffer
- **Stochastic process** describes the temporal development of a random variable

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Real system vs. model

- Typically,
 - the model describes just one part or property of the real system under consideration and even from one point of view
 - the description is not very accurate but rather approximative
- Thus,
 - caution is needed when conclusions are drawn

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Practical goals

- Network planning
 - dimensioning
 - optimization
 - performance analysis
- Network management and control
 - efficient operating
 - fault recovery
 - traffic management
 - routing
 - accounting

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Literature

- Teletraffic Theory
 - *Teletronikk* Vol. 91, Nr. 2/3, Special Issue on “Teletraffic”, 1995
 - V. B. Iversen, *Teletraffic Engineering Handbook*, <http://www.tele.dtu.dk/teletraffic/handbook/telehook.pdf>
 - J. Roberts, *Traffic Theory and the Internet*, IEEE Communications Magazine, Jan. 2001, pp. 94-99 <http://perso.rd.francetelecom.fr/roberts/Pub/Rob01.pdf>
- Queueing Theory
 - L. Kleinrock, *Queueing Systems, Vol. I: Theory*, Wiley, 1975
 - L. Kleinrock, *Queueing Systems, Vol. II: Computer Applications*, Wiley, 1976
 - D. Bertsekas and R. Gallager, *Data Networks*, 2nd ed., Prentice-Hall, 1992
 - Myron Hlynka's Queueing Theory Page <http://www2.uwindsor.ca/~hlynka/queue.html>

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- **Teletraffic models**
- Little's formula

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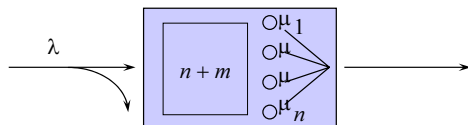
Teletraffic model types

- Three types of system models:
 - **loss systems**
 - **queueing systems**
 - **sharing systems**
- Next we will present simple teletraffic models
 - describing a single resource
- These models can be combined to create models for whole telecommunication networks
 - loss networks
 - queueing networks
 - sharing networks

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Simple teletraffic model

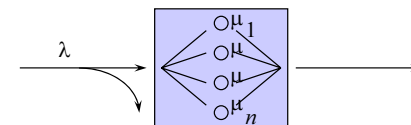
- **Customers arrive** at rate λ (customers per time unit)
 - $1/\lambda$ = average inter-arrival time
- Customers are **served** by n parallel **servers**
- When busy, a server serves at rate μ (customers per time unit)
 - $1/\mu$ = average service time of a customer
- There are $n + m$ **customer places** in the system
 - at least n **service places** and at most m **waiting places**
- It is assumed that blocked customers (arriving in a full system) are lost



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Pure loss system

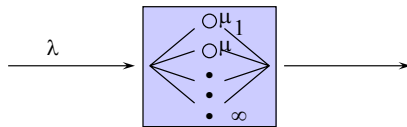
- Finite number of servers ($n < \infty$), n service places, no waiting places ($m = 0$)
 - If the system is full (with all n servers occupied) when a customer arrives, it is not served at all but lost
 - Some customers may be lost
- From the customer's point of view, it is interesting to know e.g.
 - What is the probability that the system is full when it arrives?



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Infinite system

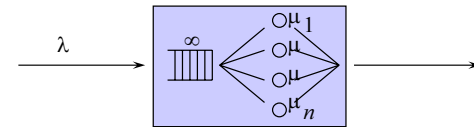
- Infinite number of servers ($n = \infty$), no waiting places ($m = 0$)
 - No customers are lost or even have to wait before getting served
- Sometimes,
 - this hypothetical model can be used to get some approximate results for a real system (with finite system capacity)
- Always,
 - it gives bounds for the performance of a real system (with finite system capacity)
 - it is much easier to analyze than the corresponding finite capacity models



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Pure queueing system

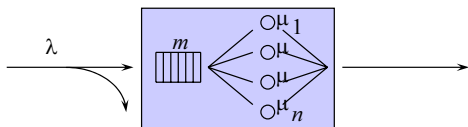
- Finite number of servers ($n < \infty$), n service places, infinite number of waiting places ($m = \infty$)
 - If all n servers are occupied when a customer arrives, it occupies one of the waiting places
 - No customers are lost but some of them have to wait before getting served
- From the customer's point of view, it is interesting to know e.g.
 - what is the probability that it has to wait "too long"?



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Lossy queueing system

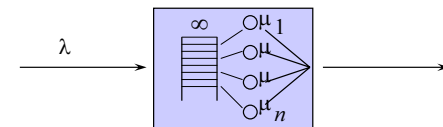
- Finite number of servers ($n < \infty$), n service places, finite number of waiting places ($0 < m < \infty$)
 - If all n servers are occupied but there are free waiting places when a customer arrives, it occupies one of the waiting places
 - If all n servers and all m waiting places are occupied when a customer arrives, it is not served at all but lost
 - Some customers are lost and some customers have to wait before getting served



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Pure sharing system

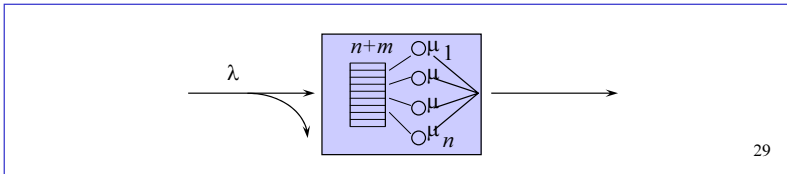
- Finite number of servers ($n < \infty$), infinite number of service places ($n + m = \infty$), no waiting places
 - If there are at most n customers in the system ($x \leq n$), each customer has its own server. Otherwise ($x > n$), the total service rate ($n\mu$) is shared fairly among all customers.
 - Thus, the rate at which a customer is served equals $\min\{\mu, n\mu/x\}$
 - No customers are lost, and no one needs to wait before the service.
 - But the delay is the greater, the more there are customers in the system. Thus, delay is an interesting measure from the customer's point of view.



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Lossy sharing system

- Finite number of servers ($n < \infty$), finite number of service places ($n + m < \infty$), no waiting places
 - If there are at most n customers in the system ($x \leq n$), each customer has its own server. Otherwise ($x > n$), the total service rate ($n\mu$) is shared fairly among all customers.
 - Thus, the rate at which a customer is served equals $\min\{\mu, n\mu/x\}$
 - Some customers are lost, but no one needs to wait before the service.

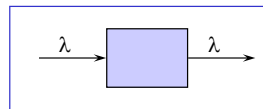


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Little's formula

- Consider a system where
 - new customers arrive at rate λ
- Assume **stability**:
 - Every now and then, the system is empty
- Consequence:
 - Customers depart from the system at rate λ
- Let
 - \bar{N} = average number of customers in the system
 - \bar{T} = average time a customer spends in the system = average delay
- **Little's formula:**



$$\bar{N} = \lambda \bar{T}$$

Proof (1)

- Let
 - $N(t)$ = the number of customers in the system at time t
 - $A(t)$ = the number of customers arrived in the system by time t
 - $B(t)$ = the number of customers departed from the system by time t
 - T_i = the time customer i spends in the system = its delay
- As $t \rightarrow \infty$,

$$\frac{1}{t} \int_0^t N(s) ds \rightarrow \bar{N}, \quad \frac{1}{A(t)} \sum_{i=1}^{A(t)} T_i \rightarrow \bar{T}, \quad \frac{1}{B(t)} \sum_{i=1}^{B(t)} T_i \rightarrow \bar{T} \quad (1)$$

- In addition (due to the stability assumption),

$$\frac{1}{t} A(t) \rightarrow \lambda, \quad \frac{1}{t} B(t) \rightarrow \lambda \quad (2)$$

Proof (2)

- We may assume that
 - the system is empty at time $t = 0$,
 - the customers depart from the system in their arrival order (FIFO)
- Then (see the figure in the following slide)

$$\sum_{i=1}^{B(t)} T_i \leq \int_0^t N(s) ds \leq \sum_{i=1}^{A(t)} T_i$$

- Thus,

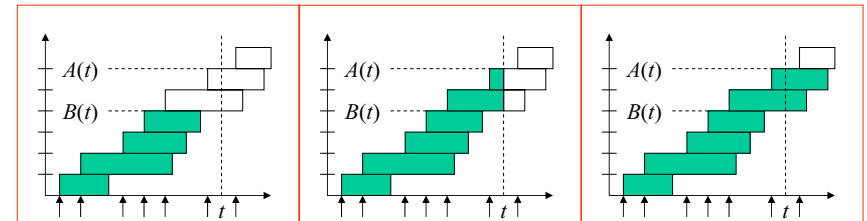
$$\frac{B(t)}{t} \frac{1}{B(t)} \sum_{i=1}^{B(t)} T_i \leq \frac{1}{t} \int_0^t N(s) ds \leq \frac{A(t)}{t} \frac{1}{A(t)} \sum_{i=1}^{A(t)} T_i$$

- As $t \rightarrow \infty$, we have, by (1) and (2),

$$\lambda \bar{T} \leq \bar{N} \leq \lambda \bar{T}$$

- Q.E.D.

Proof (3)



$$\sum_{i=1}^{B(t)} T_i$$

$$\int_0^t N(s) ds$$

$$\sum_{i=1}^{A(t)} T_i$$